

# Interactive Cloud Rendering Using Temporally-Coherent Photon Mapping

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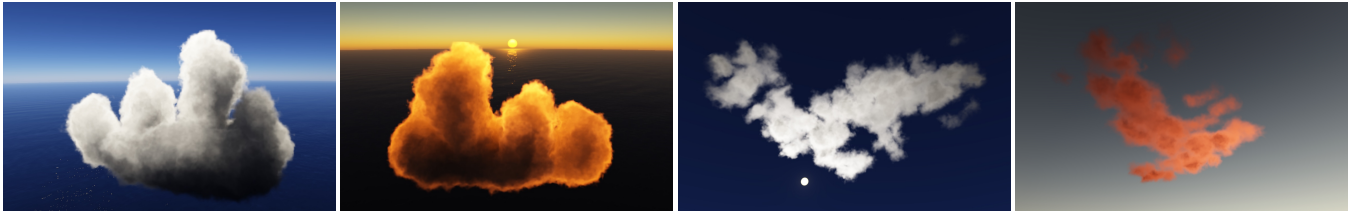


Figure 1: Cumulus congestus and Cirrocumulus altocumulus rendered fully dynamically by our approach at 25 and 35 FPS, respectively.

## ABSTRACT

This paper presents an interactive algorithm for simulation of light transport in clouds. Exploiting the high temporal coherence of the typical illumination and morphology of clouds we build on volumetric photon mapping, which we modify to allow for interactive rendering speeds — instead of building a fresh irregular photon map for every scene state change we accumulate photon contributions in a regular grid structure. This is then continuously being refreshed by re-shooting only a fraction of the total amount of photons in each frame. To maintain its temporal coherence and low variance, a low-resolution grid is used, and is then upsampled to the density field resolution in each frame. We also present a technique to store and reconstruct the angular illumination information by exploiting properties of the standard Henyey-Greenstein phase function, namely its ability to express anisotropic angular distributions with a single dominating direction. The presented method is physically-plausible, conceptually simple and comparatively easy to implement. Moreover, it operates only on the cloud density field, thus not requiring any precomputation, and handles all light sources typical for the given environment, i. e., where one of the light sources dominates.

**Index Terms:** I.3.7 [Computer Graphics]: Three-Dimensional Graphics and Realism—Raytracing; I.6.8 [Simulation and Modeling]: Types of Simulation—Monte Carlo

## 1 INTRODUCTION

Radiative transport in clouds and participating media in general is an important and broad problem. Specifically, interactive cloud rendering is often needed when an application includes interactive visualization of outdoor environments. That includes serious applications such as flight and soaring simulators or meteorological visualizations, but also popular applications, for instance 3D games and packages like Google Earth.

Among participating media, clouds stand out as a particularly difficult case for state-of-the-art volumetric light transport techniques. Their virtually unit albedo and small relative mean free photon path imply simulation of many scattering orders. The very high scat-

tering anisotropy of cloud droplets in turn causes difficulties for purely ray-based methods [37] and approaches based on discrete light propagation volumes [7, 14, 12]. The latter property in combination with the usual high complexity of cloud shapes also makes diffusion-based approaches [40, 32] unsuitable, mainly because it is usually difficult to fulfil the boundary conditions of the diffusion equation. Finally, the high variability of morphological cloud types makes it difficult to establish an efficient representation of their mass distributions. Naturally, these issues are even more challenging for interactive rendering techniques.

The method presented in this work contributes to the topic in question in these main ways:

- We present a general scheme for propagation of light energy inside participating media using photon beams. The energy is stored in a regular grid-like photon map, which is decoupled from the cloud density field. This allows a continuous updating of the photon map by re-shooting only a fraction of the photons that constitute the scene illumination in each frame. Although this potentially causes the photon map to contain a partially obsolete illumination solution, in slowly-changing environments such as clouds the difference from the ideal solution will typically be negligible.
- To avoid the necessity of explicitly storing individual photons we introduce a specialized representation of the angular illumination information. This representation accumulates the average cosine of the stored photons in respect to a reference direction (usually the direction of the strongest light source present in the scene). This accumulated value in fact is the asymmetry factor of the angular photon distribution in each cell, and is subsequently used to reconstruct the directionally-dependent illumination by evaluating the Henyey-Greenstein function parametrized by this factor and by the reference direction.
- The presented method natively maps well to modern GPUs, which we show by our own implementation. Despite not containing any specific low-level optimizations it is capable of simulating the radiative transport process in clouds at interactive speeds.

## 2 RELATED WORK

A large volume of research concerns itself with participating media and related subjects [6]. We will therefore limit ourselves to works directly relevant in the current context.

**Photon mapping** The intrinsic ability of the basic photon mapping algorithm to cache radiant energy in the scene shows to be very beneficial for participating media rendering. This application has first been described by Jensen and Christensen [21]. Later,

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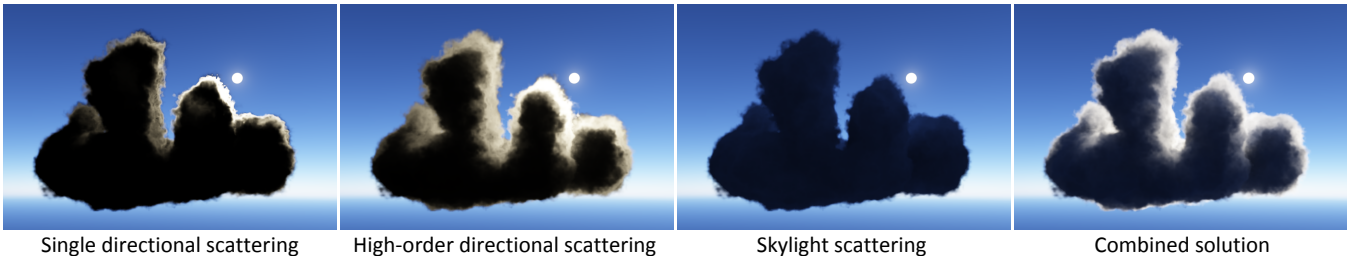


Figure 2: Decomposition of the three basic scattering categories in clouds. Note that the transition from single to second and higher orders of scattering is very subtle due to the high scattering anisotropy. For this reason methods that handle single and multiple scattering separately necessarily produce inconsistent results.

Jarosz et al. [20] developed a new beam gathering technique specifically for participating media and subsequently generalized it also for propagation of the radiant energy itself [19]. Their contribution represents a significant improvement over the classical point-based photon mapping, although it remains to be seen how it would cope with the very high amount of scattering orders encountered in clouds.

Several attempts to speed-up photon mapping by continuously updating the photon map exist. Airieau et al. [1] developed an interactive technique for continuous streaming of photons, where parts of the scene where illumination changes more rapidly are updated with higher priority. A similar (interactive) method has been described by Dmitriev et al. [8], who utilized the periodicity properties of Halton sequences to identify the photon groups to update. Jiménez et al. [22] then generalized this approach to participating media, which however causes the algorithm to perform about an order of magnitude slower than necessary for interactive frame rates. Notable GPU implementations of photon mapping were proposed by Purcell et al. [36] and Zhou et al. [47], but only Krüger et al. [27] consider participating media. Photons can be splatted to surfaces efficiently using the GPU instead of performing costly density estimations [33]. We generalize this idea to volumetric photon mapping.

**Interactive methods for general media** In recent years the increasing computational power of modern GPUs enabled development of interactive approaches for participating media rendering, although they are still burdened by various limitations.

Approaches that consider only a subset of light paths in the medium are also common, partly because they usually map well to modern GPU architectures. Often they restrict themselves to modelling single scattering, even when including advanced effects such as volumetric caustics [45, 10, 2, 29]. Ihrke et al. [17] use wavefront rendering to evaluate the Eikonal equation in volumes, considering refraction and single scattering in heterogeneous media. Kaplanyan and Dachsbacher [23] use a discrete-element approach similar to lattice-Boltzmann lighting in order to render low-frequency global illumination and low-order scattering. Shadows for single-scattering can efficiently be computed using deep shadow maps [30], which generalize binary shadow maps to storing a transmission function per pixel. Yet again, these methods are unsuitable for clouds rendering — that is simply because they neglect the higher scattering orders, which play a significant role for the appearance of clouds.

Engelhardt et al. [11] present a method based on the original instant radiosity approach by Keller [24]. Although successfully capturing appearance of several participating media, it shares the limitations of the original instant radiosity approach, namely the difficulty with handling highly anisotropic reflections and scattering.

**Precomputation and Caching** Another possible approach is caching of illumination globally for the entire volume [18, 34]; various methods from this group then differ primarily in how this is achieved. Kautz et al. [39] include simple participating media in their PRT approach, while Zhou et al. [48] use a decomposition of the

medium into a low frequency representation and a high-frequency residual field, and solve the radiative transport in the medium by applying the diffusion equation to the low-frequency field. However, these approaches rely significantly on precomputations and therefore are not suitable for dynamic media. Moreover, the illumination information is encoded into spherical harmonic functions, which are not well suited for representing highly anisotropic angular distributions.

**Cloud rendering** Although specialized methods for rendering of clouds are more typical in the interactive domain, early non-interactive methods focused on simulating this phenomenon exist. Examples of these include works by Gardner [13] and Nishita et al. [35]. These clearly demonstrate that clouds have always been of prime interest among participating media.

Though many diverse approaches for interactive clouds rendering exist, they can roughly be categorized as empirical and physically-based. From the former group we mention the typical billboard-based technique by Wang [42] used for instance in Microsoft Flight Simulator 2004 or CryEngine2 [43].

On the other hand, many different paradigms have been taken in the existing physically-based approaches. Riley et al. [38] use the half-angle slicing technique of Kniss et al. [25] known from the domain of volume visualization. The method, however, is still semi-empirical and considers only the forward portion of multiple scattering and a single light source. The concept of Monte-Carlo illumination networks by Szirmay-Kalos et al. [41] is more theoretically sound, its main drawback however is the necessity to recalculate the entire network from scratch every time the cloud density field changes. Yet another approach has been taken by Bouthors et al. [3, 4] who analyse light behaviour in plane-parallel homogeneous slabs and based on this analysis design a series of *ad-hoc* functions to obtain illumination in the rendered cloud. The method produces interesting results, it is however limited to simple light sources and builds primarily on theoretical assumptions rather than on actual observations of the simulated environment.

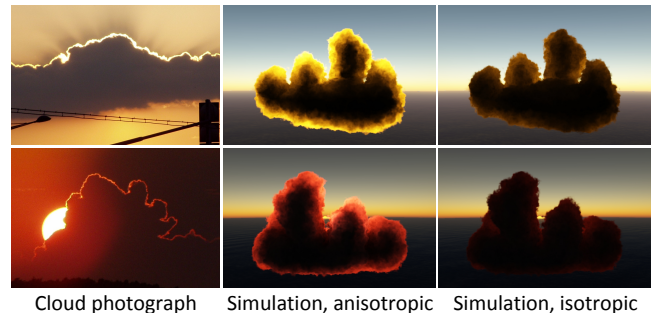


Figure 3: Anisotropic scattering is a defining visual property of clouds, causing above all the *silver lining* effect. Without correctly handling anisotropic scattering it is difficult to reproduce this phenomenon.

**Discussion** Generally, we observe that the existing methods for rendering of participating media can be categorized in yet another way. The first category are approaches that can very rapidly simulate single scattering, but handle multiple scattering either in a supplemental way or even not at all. On the other hand, approaches that handle multiple scattering using lattice-based propagation or diffusion techniques fail at reproducing low-order or highly anisotropic effects (Fig. 3). The main difficulty of clouds lies in the fact that their high scattering anisotropy makes the transition from low-order to high-order scattering effects very gradual (see Fig. 2), thus these effects need to be handled in a consistent manner. The third group of hybrid methods that use ray-based propagation of radiant energy, but cache this energy in some way, has the potential to handle the described phenomenon. Unfortunately, this is usually hindered by the use of spherical harmonics to store the angular radiance distributions, destroying any high-frequency illumination effects (or making the caching process too costly as the number of basis coefficients needed to represent increasing frequencies grows quadratically). To remedy this situation is the main target of our work.

### 3 METHOD OVERVIEW

This section provides an overview of our method. We first introduce the physical model and assumptions we use (Sec. 3.1) and then give a brief overview of the method itself (Sec. 3.2).

#### 3.1 Model

The physical model that describes the propagation of light through participating environments is mathematically described by the radiative transfer equation (RTE) [7, 31]:

$$\frac{dL(\mathbf{x}, \boldsymbol{\omega})}{d\mathbf{x}} = -\sigma_t(\mathbf{x})L(\mathbf{x}, \boldsymbol{\omega}) + \sigma_s(\mathbf{x}) \int_{\Omega_{4\pi}} p(\mathbf{x}, \boldsymbol{\omega}, \boldsymbol{\omega}')L(\mathbf{x}, \boldsymbol{\omega}') d\boldsymbol{\omega}'.$$

RTE describes differential change of radiance  $L$  at a point in space  $\mathbf{x}$  in the direction  $\boldsymbol{\omega}$ .  $\sigma_t$  and  $\sigma_s$  are the extinction and scattering cross sections of the simulated medium (in clouds we consider  $\sigma_t = \sigma_s$ ). The spherical function  $p$  is the phase function; if  $p$  is the same for the entire medium the first parameter  $\mathbf{x}$  can be omitted. In addition,  $p$  is usually considered to be rotationally symmetric around the incident direction  $\boldsymbol{\omega}$  and therefore becomes a 1D function of the angle between the incident and the outgoing direction. We employ both of these assumptions and will therefore use the notation  $p(\theta)$  interchangeably with  $p(\boldsymbol{\omega}, \boldsymbol{\omega}')$ . Since we do not consider emission in clouds our formulation of RTE does not contain an emission term.

The classical volumetric photon mapping solves the RTE by performing a random Monte Carlo walk through the medium. This however requires the ability to determine the next location where the simulated photon will interact with the medium. To obtain this location in an unbiased manner we utilize the Woodcock tracking technique [44]. Please refer to Appendix A for its brief description.

The phase function model we employ is the standard formulation by Henyey and Greenstein [16]:

$$p_{HG}(\theta, g) = \frac{1}{4\pi} \cdot \frac{1 - g^2}{(1 + g^2 - 2g \cos \theta)^{3/2}} \quad (1)$$

where  $g \in (-1, 1)$  denotes the anisotropy of  $p_{HG}$ . It is an average weighted cosine of the scattered directions produced by any given  $p$ :

$$g = \int_{\Omega_{4\pi}} p(\theta) \cos \theta d\boldsymbol{\omega}'. \quad (2)$$

There are multiple reasons why we have decided to use the Henyey-Greenstein function instead of a tabulated rigorous Mie phase function (such as for instance in Bouthors et al. [3, 4]). The Henyey-Greenstein function thanks to its closed analytical form is more

portable, cheaper to evaluate and can be efficiently importance-sampled. Moreover, we utilize its mathematical properties to represent the illumination in clouds as well (Secs. 4.1.2 and 4.4). The main drawback of using this approximation is its inability to reproduce advanced scattering effects occurring in clouds, e.g., fogbows and glories [4]. However, these phenomena are comparatively rare and can be modelled separately.

**Assumptions** At this point we establish assumptions about the environment we aim to simulate. We base these assumptions primarily on actual observations of the simulated environment, and later demonstrate how they are used to the method’s advantage.

- **Illumination.** Clouds are virtually always illuminated by a single strong yet slowly-moving light source with one *dominant direction* (the Sun or the Moon) and by additional slowly-changing environmental light sources (the sky, street lights in urbanized areas, etc.). Occurrences such as an airplane rapidly flying through a cloud are sufficiently rare and we deem acceptable to neglect them. Mathematically, this assumption can be expressed in the way that clouds are illuminated by low-frequency light sources, and that both in temporal and spatial domain.
- **Mass distribution.** Clouds are indeed dynamic media, as their shape changes due to air convection. However, not only is this process never very rapid, it is seldom even noticeable for a human observer. Movement of whole clouds across the sky due to wind is usually relatively slow as well.

Apart from these, no other assumptions are made by our approach. We allow for any type and number of light sources, as long as there is one with a dominant radiant power and direction. Even local light sources are acceptable, if they move slowly. Similarly, we allow for arbitrary cloud shapes that can be represented by a 3D discrete density field. The source of this density field can be arbitrary as well — it can be stored as a series of volumetric animation frames in memory, or can result from a dynamic cloud convection simulation. No precomputations need to be performed on these data. And finally, we do not impose any limitations on the observer orientation or movement.

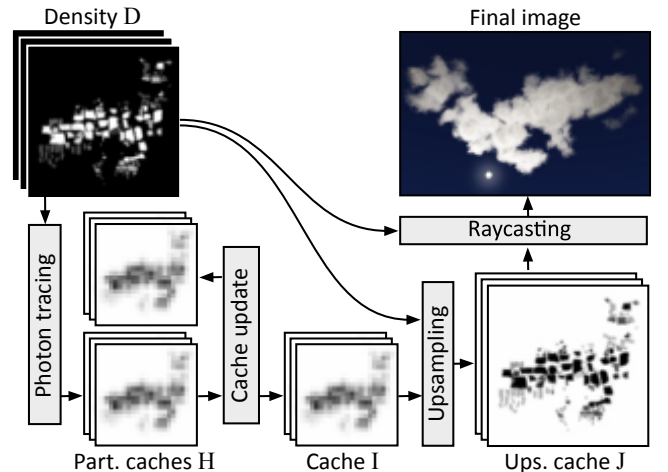


Figure 4: Schematic view of our algorithm pipeline.

#### 3.2 Overview

The input to our approach is the scalar density field of the simulated cloud, stored in a regular grid  $\mathbf{D}(i, j, k) : \mathbb{N}^3 \rightarrow \mathbb{R}^+$  (see Fig. 4). Assuming a slowly changing environment we cache illumination into another regular grid  $\mathbf{I}(i, j, k) : \mathbb{N}^3 \rightarrow \mathbb{R}^4$ . Every cell in  $\mathbf{I}$  stores the RGB flux as well as one anisotropy coefficient (Eq. 2) to model



the light distribution (Sec. 4.1.2). The grid  $\mathbf{I}$  is updated progressively, so each cell stores a mix of the current and several increasingly outdated values; however, as long as our assumptions hold, the difference from the ideal solution will be very small.

The caching data structure is a circular buffer of  $m$  (we use  $m = 20$ ) partial caches  $\mathbf{H}_0(i, j, k), \dots, \mathbf{H}_{m-1}(i, j, k)$  that combine as

$$\mathbf{I}(i, j, k) = \frac{1}{m} \sum_{l=0}^{m-1} \mathbf{H}_l(i, j, k)$$

to the full cache. The spatial resolution of the cache  $\mathbf{I}$  is much lower than the one of the density field  $\mathbf{D}$  to keep the amount of consumed memory and the variance of  $\mathbf{I}$  in low values. To improve quality, before reconstructing the final image from  $\mathbf{I}$  and  $\mathbf{D}$  using ray-marching we upsample  $\mathbf{I}$  to a second high-resolution cache  $\mathbf{J}$ , which has the same resolution as  $\mathbf{D}$ .

The global energy state of the cloud is represented by  $n_t$  photons, which are divided into  $m$  generations, each containing  $n_g = n_t/m$  photons. In each frame  $f$  the algorithm performs the following:

1. The flux of  $n_g$  photons that are shot and traced through  $\mathbf{D}$  is stored into a *new* partial cache  $\mathbf{H}_{\text{new}}$  (Sec. 4.1).
2. The partial cache  $\mathbf{H}_{\text{old}} = \mathbf{H}_{f \bmod m}$  in the circular buffer becomes the *old* partial cache and we replace it with the new partial cache  $\mathbf{H}_{\text{new}}$  as:  $\mathbf{I}^{(f)} = \mathbf{I}^{(f-1)} - \mathbf{H}_{\text{old}} + \mathbf{H}_{\text{new}}$  (Sec. 4.2).
3. The low-resolution cache  $\mathbf{I}$  is upsampled to another cache  $\mathbf{J}$  using the density field  $\mathbf{D}$  as a guidance signal (Sec. 4.3).
4. Ray-marching  $\mathbf{D}$  and  $\mathbf{J}$  produces the final image (Sec. 4.4).

In the following we present the details of each step.

## 4 OUR APPROACH

In this section we describe temporally-coherent volumetric photon mapping in more detail. We will describe it for a general fine-grained parallel machine (our implementation uses CUDA). Such a machine executes many parallel threads, can read and write into buffers, read from special buffers called “textures” that provide efficient one-, two- and three-dimensional linear filtering, and can read and write to fast “local” memory.

At the beginning of each frame the cloud density field  $\mathbf{D}$  is updated and stored into a texture, e. g., using a simulation of cloud dynamics or by streaming the dataset from memory on-the-fly.

### 4.1 Illumination

Illumination is computed by tracing photons (Sec. 4.1.1) in the density field  $\mathbf{D}$  and storing (Sec. 4.1.2) them into a new partial cache  $\mathbf{H}_{\text{new}}$ . The spatial resolution of  $\mathbf{H}$  is typically much lower than of  $\mathbf{D}$ : the number of its cells should not exceed 2400 (for a cubic grid this limits the resolution to  $13^3$ ) in order to fit into the 48 kB of shared local memory available on current GPUs.

#### 4.1.1 Photon tracing

In every step,  $n_g$  photons are shot from the Sun and the sky (note that different number of photons may be traced in each frame, e. g., if there is a need to balance time taken by other tasks performed by the GPU; the only requirement is that these photons carry the same flux, so that the energy state of the scene remains consistent). First, they are attenuated due to atmospheric scattering using a tabulated model [5, 9]. For photon propagation, we adapt the *photon marching* technique presented by Jarosz et al. [19]: for every photon a parallel thread is started and runs in a while-loop that scatters and stores photons (Sec. 4.1.2) until the photon leaves the volume. Instead of depositing photons in constant [19] or adaptively-sized [28] steps, we perform randomly-sized steps — since we employ Woodcock tracking (that itself performs randomly-spaced steps to generate interactions with the medium) for obtaining free photon path through

the medium, we deposit photons at the locations where Woodcock tracking examines the currently generated event. This essentially helps us to avoid two simultaneous stepping procedures along the propagation ray. See Fig. 5 for an illustration of this process.

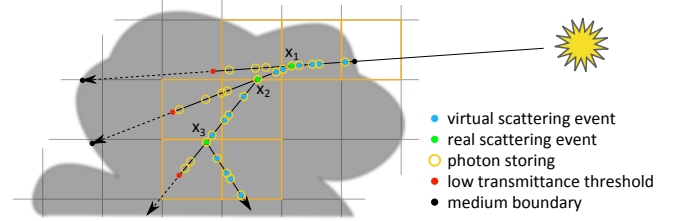


Figure 5: The scheme of our photon beam propagation procedure. Only the orange-framed grid cells receive photon energy. For details please refer to Appendix A.

In addition, the original photon marching technique traces each photon beam up to the medium boundary. Such an approach is indeed suitable for optically thin media such as fog and certain kinds of smoke which Jarosz et al. [19] use in their demonstrations. However, in optically thick environments, such as clouds, this approach invests large amounts of computational effort into simulating and storing photons that—due to low medium transmittance—carry only very little energy. To overcome this problem we simply stop tracing a beam if its transmittance gets below a small threshold. Although this of course introduces a slight bias, our experiments show that the resulting speed-up can even reach an order of magnitude.

Further, we use the similarity theory [46] to speed up the tracing process. We pose a fixed threshold  $t$  (for instance  $t = 0.05$ ) and if the cumulated scattering anisotropy of a traced photon gets below  $t$ , we switch to the reduced scattering cross section  $\sigma'_s = \sigma_s \sqrt{1-g}$ . In our case it is easy to determine this, because the angular distribution of light scattered  $i$  times corresponds to  $i$  self-convolutions of the phase function, which for Henyey-Greenstein function in turn corresponds to just using  $g^i$  instead of  $g$  as its anisotropy parameter [32]. Therefore for a given photon we switch to  $\sigma'_s$  after  $i = \log(t)/\log(\max(g, \epsilon))$  bounces (for a small  $\epsilon > 0$ ).

#### 4.1.2 Photon storing

The classical (volumetric) photon mapping [21] and volume irradiance caching [18] both have two shortcomings that hinder their application to interactive cloud rendering: maintaining and querying of complex spatial data structures and limited support for highly-anisotropic scattering due to spherical harmonic functions used for the caching. Our approach overcomes both limitations by using a simple regular grid and a different basis function.

**Regular photon grids** Classic volumetric photon mapping stores volumes into hierarchical data-structures, such as kD-trees, that can adaptively resolve fine spatial details in the photon distribution as found, e. g., in occlusions or caustics in surface lighting. For clouds however, fine spatial details are usually absent. On the other hand, inserting photons into a complex structure and performing an adaptive density estimation is less suitable for contemporary massively-parallel machines which we target. We therefore suggest to trade adaptivity for simplicity and revert to a plain regular grid in which the illumination is accumulated, similar to irradiance volumes [15] (also see Fig. 5). This grid  $\mathbf{H}$  is sufficiently small to fit into local memory shared by a block of threads executed on one multi-processor. Storing a photon into such a three-dimensional grid is now as efficient as splatting it in two dimensions [33]. Also, as atomic operations are necessary to perform the accumulation properly, for the fast local shared memory we found them not to cause virtually any additional overhead.



Sec. 4.3 explains how an upsampling scheme can be used to improve the effective spatial resolution of the cache.

**Henye-Greenstein basis** Approaches that cache the illumination information inside the volume [18, 34] use spherical harmonics to approximate the radiance function. This is suitable for isotropic and moderately anisotropic media, but not for strongly forward-scattering media such as clouds, where a high number of SH coefficients is required. This is problematic, as the strong forward scattering in clouds is visually important for their appearance, for instance causing the well known *silver lining* phenomenon (Fig. 3).

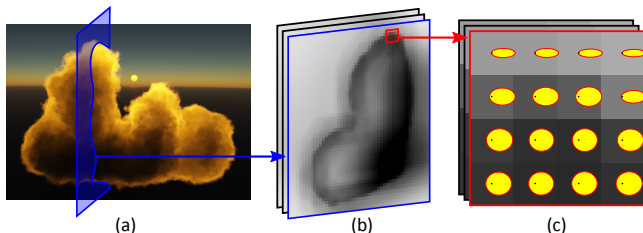


Figure 6: Local Henye-Greenstein lobes — (b) shows one slice of the grayscale-encoded anisotropy coefficients of the illumination solution that correspond to the marked region on the cloud (a). The exact shape of the lobes in the cache locations is shown in (c). The light in (c) is coming from the left.

To overcome this limitation we propose to represent caches using the Henye-Greenstein function (Eq. 1). Evidence shows [17] that in situations where most energy in scene comes from a single direction then also a majority of scattered light will propagate in a very similar direction, which will be especially true for clouds. Thus, when storing a photon into a cache cell, in addition to its radiant flux we also accumulate its cosine with respect to the dominant light direction. This only requires to store four values (an RGB-triple for flux and a single cosine value) per cell and the projection consists of evaluating just a single dot product per photon. In addition we count the number of photons arriving at each cell, and after all photons are shot, divide the accumulated cosines by the number of contributing photons for a proper normalization. The value obtained this way is anisotropy factor for the given cache cell (Eq. 2). We can then directly use the Henye-Greenstein function to represent the per-cell angular illumination distribution (Fig. 6).

Photons which are not emitted by the Sun but from the sky are projected into the same HG basis. As they—in difference from the Sun photons—arrive from a wide distribution of directions, their angular contribution to the caches is close to uniform and thus does not require consideration of an additional reference direction. Naturally, in scenarios where the sky contributes a significant portion of energy (e. g., after sunset or in optically thicker atmospheres), this can decrease the anisotropy of the HG lobes too much. In such situations one could simply store only the intensity of these environmental photons separately and regard them as having a uniform angular distribution.

## 4.2 Update

After computing the cloud illumination using the photon tracing explained before, the partial cache  $\mathbf{H}_{\text{new}}$  is added to the global solution  $\mathbf{I}$  and the outdated cache  $\mathbf{H}_{\text{old}}$  is removed. This is done using a simple parallel addition and subtraction over all cache cells.

## 4.3 Upsampling

At this point  $\mathbf{I}$  could already be used for rendering. However, it is of much lower spatial resolution than  $\mathbf{D}$ . This was required to fit it into shared local memory and to reduce variance of the illumination solution (see Appendix B). However, the low spatial resolution of

the cache  $\mathbf{I}$  can substantially blur the illumination and cause interpolation artefacts. To avoid this limitation, we propose to upsample  $\mathbf{I}$  to  $\mathbf{J}$ , a grid with the same spatial resolution as  $\mathbf{D}$  (Fig. 7). We use  $\mathbf{D}$  as a guidance signal and apply joint bilateral upsampling [26] to avoid blurring over its edges. This approach provides empirically good results, which is not unexpected as it can be assumed that in clouds the density field  $\mathbf{D}$  and the scattered radiance function  $L_{\text{out}}$  (Sec. 4.4) will spatially correlate on a local scale (roughly within one photon mean free path distance).

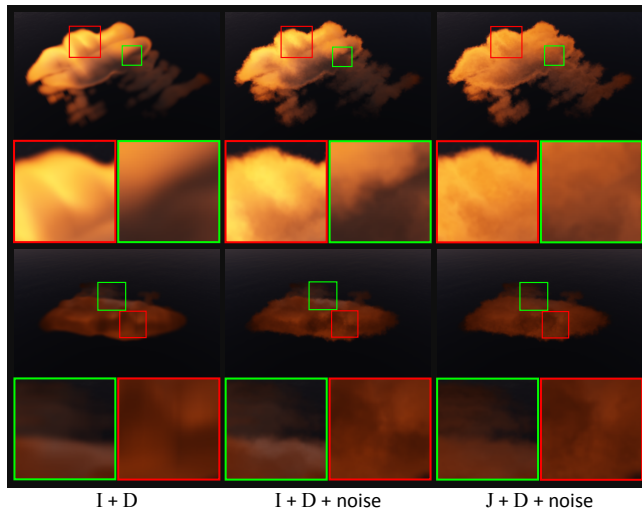


Figure 7: The importance of upsampling the coarse illumination solution  $\mathbf{I}$ . Although noise perturbation helps break the unnatural smoothness of  $\mathbf{D}$ , it does not remove some abrupt artefacts caused by linear interpolation of  $\mathbf{I}$ .

The upsampling maps well to GPUs — it is a purely local operation executed in parallel exactly once per each upsampled solution cell using a  $3^3$  Gaussian filter. The upsampling could also be performed directly during the ray-marching, but we found it to be much faster when done in an intermediate step.

## 4.4 Ray-marching

To visualize clouds we use the standard ray-marching [28] with early-exit at 2% transmittance threshold. For every pixel, a thread is started that marches  $\mathbf{D}$  and  $\mathbf{J}$ , accumulates radiance from  $\mathbf{J}$  (see below) and transmittance  $T$  from  $\mathbf{D}$  in front-to-back order, applies compositing accordingly and terminates when  $T$  is less than 2%.

To keep the memory consumption in manageable levels we use only moderate resolutions for  $\mathbf{D}$  (see Table 1). We then increase the amount of detail by procedural perturbation of the texture coordinates for fetching  $\mathbf{D}$  and  $\mathbf{J}$  by three octaves of simple vector noise stored in a small 3D texture, similar to Kniss et al. [25] (Fig. 7).

For most clouds it is not necessary to ray-march them in full screen resolution, as the frequency of the applied noise is still lower than the screen sampling frequency (see Fig. 10, left). Therefore in all cases we render the cloud in half the screen resolution, in both dimensions. Additional speed-ups could easily be achieved by using cloud impostors.

**Reconstruction** The illumination reconstruction is straightforward at this moment.  $\mathbf{J}$  contains four values in each cell — an RGB intensity of the illumination energy and the local anisotropy factor  $g'$ , which represents the angular distribution of this energy.

It is however important to note that since we use the incident photon direction for the projection step during the photon tracing procedure (Sec. 4.1.1), the value of  $g'$  represents the *incident* radiance function  $L_{\text{in}}$  at the cache location. To obtain the desired *outgoing*

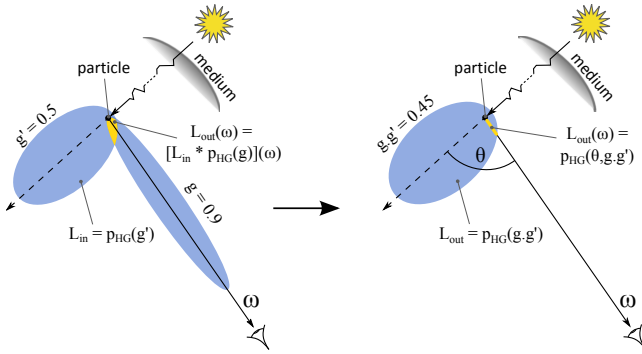


Figure 8: Two possible ways of reconstructing the illumination information represented by the Henyey-Greenstein function. Left: the yellow area represents the value of  $L_{out}(\omega)$  obtained by convolving  $L_{in}$  and  $p_{HG}(g)$ . Right: the yellow segment is directly the value of  $L_{out}(\omega)$ .

radiance value  $L_{out}(\omega)$  for a given view direction  $\omega$  it is necessary to convolve  $L_{in}$  (represented by  $p_{HG}(g')$ ) with the medium phase function centred around the viewing direction (Fig. 8, left). Instead of computing the convolution directly (e. g., numerically) we once more utilize the self-convolution property of the Henyey-Greenstein function (Sec. 4.1.1) — and simply evaluate  $p_{HG}(\theta, g \cdot g')$ , where  $g$  is the global anisotropy factor used for scattering simulation in the cloud (Fig. 8, right). This is mathematically equivalent (see Appendix C).

An additional benefit of our Henyey-Greenstein representation is that the angular illumination information represented this way reproduces the scattering anisotropy in clouds well, but at the same time is smooth. This prevents emergence of any high-frequency noise, which would look very unnatural in clouds.

## 5 RESULTS AND DISCUSSION

Our tests have been conducted on a laptop PC with 2 GHz Intel Core i7-2630QM CPU, Nvidia GTX 485M GPU and Windows 7 64-bit. In all our tests we use the following global settings: 400 k photon beams,  $m = 20$  partial caches, ray-marching step size of  $d/300$  (where  $d$  is the cloud bounding box diagonal) and a screen resolution of  $1920 \times 1200$ . We have performed two kinds of tests — method performance measurements and analysis of the illumination outdated during scene state change.

**Performance** We have used three datasets for timing measurements: static datasets of Cumulus congestus (dense concentrated cloud) and Altostratus undulatus (sparse wavy cloud) and an animated smoke dataset available in PBRT renderer ([pbrt.org](http://pbrt.org)). The scene settings and measured timings are summarized in Table 1. Figs. 1, 10 (right) and 11 show the results of our method, including the measured datasets. All density fields beside the PBRT smoke were modelled by hand as meshes and voxelized into 3D grids.

**Illumination obsolescence** Since our method amortizes the illumination computation there is a various level of obsolescence in the partial solutions. To show that our update process is sufficiently fast we compare clouds rendered under constant light source movement against clouds under static illumination. Fig. 9 shows the resulting images. The maximal luminance difference in the evening (when the illumination changes most rapidly) was 13 %, but there is no observable difference between the results. During the day the difference is completely negligible (under 3 %). Please note that although the Sun’s angular speed was only 0.5 deg / s this is still 120 times faster than the real-time speed and several times faster than is commonly used in interactive 3D applications (for instance the common time ratio in FPS games is 1 game-time hour to 2 real-time minutes, which corresponds to an angular speed of 0.125 deg / s).

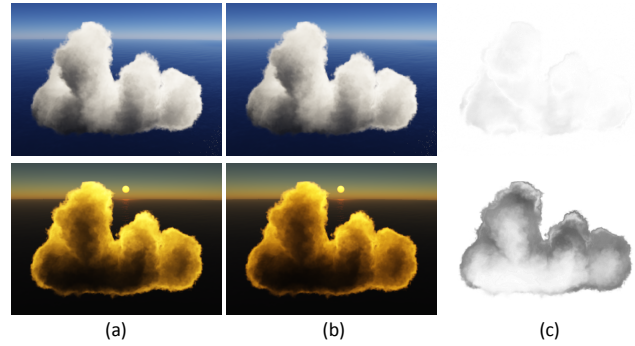


Figure 9: Illumination obsolescence in Cumulus congestus cloud during day and in the evening. (a): Sun moving in 0.5 deg/s vertically. (b): stationary Sun. (c): difference  $\times 5$  (dark-hot).

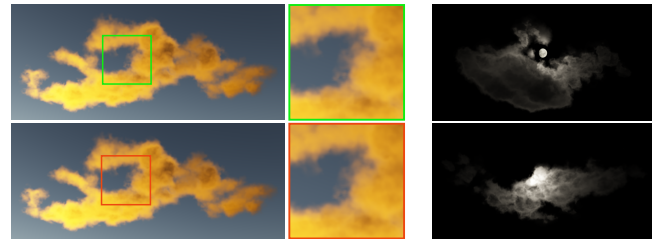


Figure 10: Left: Cirrocumulus altocumulus rendered at full resolution (top, ray-marching time 77 ms) and half resolution (bottom, ray-marching time 21 ms). Right: clouds rendered at night.

## 6 CONCLUSION AND FUTURE WORK

We have presented an interactive cloud rendering method. Our algorithm utilizes a temporally-coherent illumination caching process to amortize the simulation costs across multiple frames. Our novel representation of angular illumination distribution inside clouds enables us to reproduce the characteristic appearance of many clouds, while keeping the computational and storage costs relatively modest. The algorithm maps very well to the architecture of modern graphics hardware, and hence all its major steps can be evaluated in parallel on the GPU.

The proposed method improves on the existing techniques in multiple regards. We build on realistic observations about the typical environment of clouds and use these to our advantage. Our method is not limited to any particular cloud type or any subset of possible light paths in clouds, and can handle all important light sources typical for the simulated environment. We consider all physically plausible properties of clouds and the entire method is physically meaningful and conceptually simple.

The possible future work includes several directions. First, there is need for a multiresolution scheme to enable simulation of multiple clouds at once without linear decrease in speed. Second, the algorithm might possibly be adapted to other types of participating media by relaxing or even completely dropping the specific assumptions about the simulated environment. For example, multiple HG lobes could be used to represent more complex illumination distributions than the one dealt with in the described approach. It remains to be seen to what extent is this feasible.

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Table 1: Performance of our algorithm in various stages. All other steps took less than 1 ms to execute, thus we don't list them.

Dataset	D resolution	D size (km)	$\sigma_s$ (m <sup>-1</sup> )	$g$	I resolution	Photon tracing	Upsampling	Ray-marching	Total
Altostratus undulatus	70×22×71	1.40×0.44×1.42	0.03	0.96	18×6×18	9.5 ms	2.3 ms	14.0 ms	25.8 ms
Cumulus congestus	48×62×90	0.94×1.22×1.78	0.03	0.96	10×12×18	17.1 ms	3.0 ms	20.4 ms	40.5 ms
PBRT smoke (anim.)	100×40×100	2×0.8×2	0.05	0.95	18×7×18	19.7 ms	3.3 ms	37.8 ms	60.8 ms



Figure 11: More results of our method. In reading order, by pairs: Altostratus undulatus, Cumulus humilis, Cumulonimbus incus, Stratocumulus and the PBRT smoke dataset.

## REFERENCES

- [1] B. Airieau, D. Meneveaux, F. Bridault, and P. Blasi. Photon streaming for interactive global illumination in dynamic scenes. *Visual Computer*, 27:229–240, 2011.
- [2] I. Baran, J. Chen, J. Ragan-Kelley, F. Durand, and J. Lehtinen. A hierarchical volumetric shadow algorithm for single scattering. In *ACM Trans. Graph. (Proc. SIGGRAPH)*, volume 29, 2010.
- [3] A. Bouthors, F. Neyret, and S. Lefebvre. Real-time realistic illumination and shading of stratiform clouds. In *Proc. Workshop on Natural Phenomena*, 2006.
- [4] A. Bouthors, F. Neyret, N. Max, E. Bruneton, and C. Crassin. Interactive multiple anisotropic scattering in clouds. In *Proc. I3D*, 2008.
- [5] E. Bruneton and F. Neyret. Precomputed atmospheric scattering. In *Proc. EGSR*, 2008.
- [6] E. Cerezo, F. Pérez-Cazorla, X. Pueyo, F. J. Seron, and F. Sillion. A survey on participating media rendering techniques. *Visual Comput.*, 21:303–328, 2005.
- [7] S. Chandrasekhar. *Radiative transfer*. Dover Publications, 1960.
- [8] K. Dmitriev, S. Brabec, K. Myszkowski, and H.-P. Seidel. Interactive global illumination using selective photon tracing. In *Proc. EGRW*, pages 25–36, 2002.
- [9] O. Elek and P. Knoch. Real-time spectral scattering in large-scale natural participating media. In *Proc. SCCG*, pages 77–84, 2010.
- [10] T. Engelhardt and C. Dachsbacher. Epipolar sampling for shadows and crepuscular rays in participating media with single scattering. In *Proc. I3D*, pages 119–125, 2010.
- [11] T. Engelhardt, J. Novák, and C. Dachsbacher. Instant multiple scattering for interactive rendering of heterogeneous participating media. Technical report, Karlsruhe Institut of Technology, December 2010.
- [12] R. Fattal. Participating media illumination using light propagation maps. *ACM Trans. Graph.*, 28:7:1–7:11, 2009.
- [13] G. Y. Gardner. Visual simulation of clouds. In *Proc. SIGGRAPH*, pages 297–304, 1985.
- [14] R. Geist, K. Rasche, J. Westall, and R. Schalkoff. Lattice-Boltzmann lighting. In *Proc. EGSR*, pages 355–362, 2004.
- [15] G. Greger, P. Shirley, P. Hubbard, and D. Greenberg. The irradiance volume. *Computer Graphics and Applications, IEEE*, 18(2), 1998.
- [16] L. G. Henyey and J. L. Greenstein. Diffuse radiation in the Galaxy. *Astrophysical Journal*, 93(1):70–83, 1941.
- [17] I. Ihrke, G. Ziegler, A. Tevs, C. Theobalt, M. Magnor, and H.-P. Seidel. Eikonal rendering: efficient light transport in refractive objects. *ACM Trans. Graph. (Proc. SIGGRAPH)*, 26, 2007.
- [18] W. Jarosz, C. Donner, M. Zwicker, and H. W. Jensen. Radiance caching for participating media. *ACM Trans. Graph.*, 27:7:1–7:11, 2008.
- [19] W. Jarosz, D. Nowrouzezahrai, I. Sadeghi, and H. W. Jensen. A comprehensive theory of volumetric radiance estimation using photon points and beams. *ACM Trans. Graph.*, 30:5:1–5:19, 2011.
- [20] W. Jarosz, M. Zwicker, and H. W. Jensen. The beam radiance estimate for volumetric photon mapping. *Computer Graphics Forum (Proc. Eurographics)*, 27(2):557–566, 2008.
- [21] H. W. Jensen and P. H. Christensen. Efficient simulation of light transport in scenes with participating media using photon maps. In *Proc. SIGGRAPH*, pages 311–320, 1998.
- [22] J.-R. Jiménez, K. Myszkowski, and X. Pueyo. Interactive global illumination in dynamic participating media using selective photon tracing. In *Proc. SCCG*, pages 211–218, 2005.
- [23] A. Kaplanyan and C. Dachsbacher. Cascaded light propagation volumes for real-time indirect illumination. In *Proc. I3D*, 2010.
- [24] A. Keller. Instant radiosity. In *Proc. SIGGRAPH*, pages 49–56, 1997.
- [25] J. Kniss, S. Premoze, C. Hansen, and D. Ebert. Interactive translucent volume rendering and procedural modeling. In *Proc. Visualization*, pages 109–116, 2002.
- [26] J. Kopf, M. F. Cohen, D. Lischinski, and M. Uyttendaele. Joint bilateral upsampling. *ACM Trans. Graph. (Proc. SIGGRAPH)*, 26(3), 2007.



- [27] J. Krüger, K. Bürger, and R. Westermann. Interactive screen-space accurate photon tracing on GPUs. In *Proc. EGSR*, 2006.
- [28] J. Krüger and R. Westermann. Acceleration techniques for GPU-based volume rendering. In *Proc. IEEE Visualization*, 2003.
- [29] G. Liktov and C. Dachsbacher. Real-time volumetric caustics with projected light beams. *Proc. I3D*, 2011.
- [30] T. Lokovic and E. Veach. Deep shadow maps. In *Proc. SIGGRAPH*, pages 385–392, 2000.
- [31] N. Max. Optical models for direct volume rendering. *IEEE Trans. Vis. and Computer Graphics*, 1:99–108, 1995.
- [32] N. Max, G. Schussman, R. Miyazaki, K. Iwasaki, and T. Nishita. Diffusion and multiple anisotropic scattering for global illumination in clouds. *J. WSCG*, 1–3, 2004.
- [33] M. McGuire and D. Luebke. Hardware-accelerated global illumination by image space photon mapping. In *Proc. HPG*, 2009.
- [34] J. T. Moon, B. Walter, and S. Marschner. Efficient multiple scattering in hair using spherical harmonics. *ACM Trans. Graph.*, 27:31:1–31:7, 2008.
- [35] T. Nishita, Y. Dobashi, and E. Nakamae. Display of clouds taking into account multiple anisotropic scattering and sky light. In *Proc. SIGGRAPH*, pages 379–386, 1996.
- [36] T. Purcell, C. Donner, M. Cammarano, H. Jensen, and P. Hanrahan. Photon mapping on programmable graphics hardware. In *Proc. Graphics Hardware*, pages 41–50, 2003.
- [37] M. Raab, D. Seibert, and A. Keller. Unbiased global illumination with participating media. In *Proc. Monte Carlo and Quasi-Monte Carlo Methods*, pages 591–606, 2006.
- [38] K. Riley, D. S. Ebert, M. Kraus, J. Tessendorf, and C. D. Hansen. Efficient rendering of atmospheric phenomena. In *Proc. EGSR*, 2004.
- [39] P. Sloan, J. Kautz, and J. Snyder. Precomputed radiance transfer for real-time rendering in dynamic, low-frequency lighting environments. In *ACM Trans. Graph. (Proc. SIGGRAPH)*, volume 21, 2002.
- [40] J. Stam. Multiple scattering as a diffusion process. In *Proc. EGWR*, pages 41–50, 1995.
- [41] L. Szirmay-Kalos, M. Sbert, and T. Umenhoffer. Real-time multiple scattering in participating media with illumination networks. In *Proc. EGSR*, 2005.
- [42] N. Wang. Realistic and fast cloud rendering. In *J. Graphics, GPU & Game Tools*, 2003.
- [43] C. Wenzel. Real-time atmospheric effects in games. In *SIGGRAPH Course*, pages 113–128, 2006.
- [44] E. Woodcock, T. Murphy, P. Hemmings, and T. Longworth. Techniques used in the GEM code for Monte Carlo neutronics calculations in reactors and other systems of complex geometry. In *Proc. Application of Computing Methods to Reactor Problems*, pages 557–579, 1965.
- [45] C. Wyman and S. Ramsey. Interactive volumetric shadows in participating media with single-scattering. In *Proc. IEEE Interactive Ray Tracing*, pages 87–92, 2008.
- [46] D. R. Wyman, M. S. Patterson, and B. C. Wilson. Similarity relations for the interaction parameters in radiation transport. *Applied Optics*, 28(24):5243–5249, 1989.
- [47] K. Zhou, Q. Hou, R. Wang, and B. Guo. Real-time kd-tree construction on graphics hardware. In *ACM Trans. Graph. (Proc. SIGGRAPH Asia)*, volume 27, page 126, 2008.
- [48] K. Zhou, Z. Ren, S. Lin, H. Bao, B. Guo, and H.-Y. Shum. Real-time smoke rendering using compensated ray marching. In *ACM Trans. Graph. (Proc. SIGGRAPH)*, pages 36:1–36:12, 2008.

## A WOODCOCK TRACKING

One of the core operations performed by volumetric photon mapping is finding the distance to a next scattering or absorption event. We utilize Woodcock tracking to do this in an unbiased manner. Let us assume the last scattering event occurred at  $\mathbf{x}_k$  and the generated (normalized) scattering direction according to  $p$  is  $\omega$ . The next interaction will take place at  $\mathbf{x}_{k+1} = \mathbf{x}_k + d_{\text{event}} \cdot \omega$ . For heterogeneous media, to obtain the distance  $d_{\text{event}}$  one needs to solve the implicit equation

$$\int_0^{d_{\text{event}}} \sigma_t(\mathbf{x}_k + t \cdot \omega) dt = -\ln(1 - \xi)$$

where  $\xi$  is an uniformly distributed unit random variable.

Basically, Woodcock tracking steps along the photon propagation direction using steps with random exponentially-distributed length with the mean  $1/\sigma_T$  (where  $\sigma_T$  is the peak extinction cross section value throughout the entire medium). The technique then in each step probabilistically decides if an interaction takes place at the given position (i. e., if the currently generated event is *real* or just *virtual*), so that the distance to the generated interaction event has the mean value of  $d_{\text{event}}$  as defined the above equation. Finally, Russian roulette with the probability of  $\sigma_s(\mathbf{x}_{k+1})/\sigma_t(\mathbf{x}_{k+1})$  is used to decide if the generated interaction is scattering or absorption (this last step is skipped for clouds as  $\sigma_t = \sigma_s$ ). For more details please refer to Raab et al. [37].

## B TEMPORAL COHERENCE

In order to avoid low frequency temporal noise in the rendered images it is necessary to maintain a low variance of the illumination solution  $\mathbf{I}$ . As the convergence rate of a Monte Carlo estimate is  $O(1/\sqrt{n})$ , to maintain 2% error in each grid cell the total number of photons in scene  $n_t$  needs to be set so that each cell in  $\mathbf{I}$  receives at least around  $n \approx 2500$  photons (together from all partial caches  $\mathbf{H}_0, \dots, \mathbf{H}_{m-1}$ ). Since the photon budget is roughly fixed, the grid resolution needs to be adjusted accordingly to fulfill this criterion (in addition to the limitation imposed by the available shared memory of GPUs, see Sec. 4.1).

Note however that it is necessary to differentiate between photon beams and individual photons — a single photon beam can dispose many photons into the grid (Fig. 5). There is no precise way to determine the ratio between these two for a particular nontrivial dataset, but a good initial approximation is easily derived from the scattering cross section  $\sigma_s$ , the average density of the utilized dataset and its spatial dimensions.

## C ILLUMINATION RECONSTRUCTION

Recalling the radiative transport equation described in Sec. 3.1:

$$\frac{dL(\mathbf{x}, \omega)}{d\mathbf{x}} = -\sigma_t(\mathbf{x})L(\mathbf{x}, \omega) + \sigma_s(\mathbf{x}) \int_{\Omega_{4\pi}} p(\mathbf{x}, \omega, \omega')L(\mathbf{x}, \omega') d\omega'$$

it can be seen from the definition that the integral term on the right is a spherical convolution between the incident radiance (hereinafter  $L_{\text{in}}$ ) and the medium phase function  $p$  at  $\mathbf{x}$ .

In our approach we represent  $L_{\text{in}}$  by approximating the incident photons' flux by the  $p_{\text{HG}}$  basis function by averaging their cosine values in respect to the dominant Sun direction, thus producing an anisotropy factor  $g'$  representing the angular distribution of scattered photons at  $\mathbf{x}$  (Sec. 4.1.2). Therefore  $L_{\text{in}} \approx p_{\text{HG}}(g')$  and the integral term becomes

$$\int_{\Omega_{4\pi}} p(\omega, \omega')p_{\text{HG}}(\omega', g') d\omega',$$

neglecting the location from now on. Note that the orientation of  $p_{\text{HG}}(g')$  in space is given by the dominant light direction which is constant for the entire cloud (although nothing prevents the orientation from varying in space by simply storing the direction separately for each cell).

If the used medium phase function is also  $p_{\text{HG}}$  parametrized by some  $g$ , then utilizing the self convolution property of  $p_{\text{HG}}$  [32] (Sec. 4.1.1) we can write

$$\left[ \int_{\Omega_{4\pi}} p_{\text{HG}}(\omega, \omega', g)p_{\text{HG}}(\omega', g') d\omega' \right] (\omega) = p_{\text{HG}}(\omega, g \cdot g').$$

Thus  $p_{\text{HG}}(g \cdot g')$  represents the outgoing radiance function:

$$L_{\text{out}} \approx p_{\text{HG}}(g \cdot g').$$